Gödel spaces and perfect MV-algebras

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It is shown that the category of Gödel spaces **GS** (with strongly isotone maps as morphisms), which is dually equivalent to the category of Gödel algebras, is transferred by a contravariant functor *H* into the category $\mathbf{MV}(\mathbf{C})^{\mathbf{G}}$ of MV-algebras generated by perfect MV-chains via direct products, subalgebras and direct limits. And, conversely, by means of a contravariant functor *P* the category $\mathbf{MV}(\mathbf{C})^{\mathbf{G}}$ is transferred onto the category **GS**. Moreover, it is shown that the functor *H* is faithful and the functor *P* is full. Furthermore, both functors are dense. The description of finite coproducts of algebras which are isomorphic to Chang's algebra is given. Using duality a description of projective algebras in $\mathbf{MV}(\mathbf{C})^{\mathbf{G}}$ is given.