Memoirs on Differential Equations and Mathematical Physics VOLUME 49, 2010, 1–19



Seventieth Birthday Anniversary of Academician Nikolai A. Izobov

On January 22, 2010 Nikolaĭ Alekseyevich Izobov, member of Editorial Board of our journal, a well-known mathematician, Academician of the National Academy of Sciences of Byelorussia, Professor, Doctor of Physics and Mathematics, Winner of the State Prize of Republic of Byelorussia, became 70 years of age.

N. A. Izobov was born in Krasyni village of Lioznensk district, Vitebsk oblast of Byelorussia. In 1958 he left the Yanovichi secondary school with gold medal and in 1965 he graduated from the Faculty of Mathematics of the Byelorussian State University, majoring in differential equations. Still a student, N. A. Izobov was awarded the medal "For the Best Scientific Student Work" at the All-Union Competition of Student Works for the results obtained in a course of investigations of the structure of sets of Perron's lower exponents of linear differential systems.

In 1966, N. A. Izobov continued his post-graduate studies (under supervision of Professor Yu. S. Bogdanov) and in 1967 he defended his Candidate's Thesis. Since 1969, during 22 years he was Deputy Editor-in-Chief of the All-Union Journal "Differential Equations", of which the first 12 years he was the staff deputy, remaining a member of the Editorial Board of the journal for all subsequent years. After having defended in 1979 his Doctor's Thesis and being elected in 1980 Corresponding Member of the Academy of Sciences of Byelorussian SSR, he been working at the Mathematical Institute of National Academy of Sciences of Byelorussia successively as a senior researcher (1980–1986), Head of the Laboratory of Stability Theory (1986-1993) and Head of the Department of Differential Equations (from 1993 up to now). In 1994 we was elected Academician of the Academy of Sciences of Byelorussia. In 1996–1999, N. A. Izobov headed the Chair of Higher Mathematics of the Byelorussian State University.

The main areas of N. A. Izobov's scientific investigations are the theory of Lyapunov's characteristic exponents, the theory of stability according to a linear approximation, linear Coppel–Conti systems, Emden–Fowler equations and Linear Pfaff systems.

The Theory of Lyapunov's Characteristic Exponents. In his first works [1,2, see also 61] included in the Candidate's Thesis [6], N. A. Izobov has established that almost all solutions of an *n*-dimensional ordinary linear differential system with bounded piecewise continuous coefficients, starting at a *k*-dimensional (k = 1, ..., n) hyperplane of the space \mathbb{R}^n , have the lower Perron's exponent equal to the maximal one of the lower exponents of those solutions. He also proved that there exist linear systems whose set of lower Perron's exponents has the power of the continuum [2] and of positive Lebesgue measure. Thus he has established principal distinctions between the structure of the sets of Lyapunov's characteristic exponents and Perron's lower exponents. Later on, these systems were used by E. A. Barabanov for a complete description of sets of lower exponents. Recently, N. A. Izobov [140, 142], jointly with A. B. Filiptsov, proved that, in particular, the maximal Perron's lower exponent of a linear differential system coincides with the Perron's lower exponent of its fundamental system of solutions.

Concerning the freezing method which traces back to P. Bohl, N. A. Izobov proved [18] that in the two-dimensional case his basic estimate – the Alekseyev–Vinograd estimate of the highest characteristic exponent of linear non-stationary system is attainable (in the *n*-dimensional case this fact was established later by Yu. I. Elefteriadi). N. A. Izobov also obtained more precise versions of that estimate as well as its integral version for twodimensional [16–19] and *n*-dimensional [22, 43] linear differential systems. The freezing method closely relates to the construction [22] of a normal system of solutions of the *n*-dimensional linear differential system with the coefficient matrix which has the maximal norm $\delta > 0$ of its derivative on the positive semi-axis and whose eigen-values $\lambda_k(t)$ are real and separated from each other by a constant $\Delta > 0$. For the constructed normal system of solutions, in the domain $\Delta \geq \delta^{1/(2n-1)}$ there were obtained non-improvable estimates of the angle deviations between the corresponding solutions and eigen-vectors of the coefficient matrix (by the constant $const \times \delta \Delta^{2/(1-n)}$), as well as the estimates (by the function $\exp 2\delta \Delta^{2/(1-n)}t$) of the ratios of the norms of these solutions and the functions $\exp \int_0^t \lambda_k(\tau) d\tau$. To the freezing method relates also the proof [20] of reducibility (by means of a Lyapunov transformation) of a general two-dimensional linear system to an almost diagonal one whose out-of-diagonal elements do not exceed by absolute value the exact constant $const \times \delta^{1/(1+n)}$.

Concerning the problem on stability of Lyapunov's characteristic exponents of a linear differential system with respect to small perturbations which traces back to Perron, jointly with B. F. Bylov and independently of V. M. Millionshchikov (but applying his method of rotations), N. A. Izobov obtained [11, 12] a criterion of their stability (the sufficiency of that criterion had been established earlier in the well-known monograph due to B. F. Bylov, et al. "The Theory of Lyapunov's exponents"). In [21], N. A. Izobov obtained also a coefficient criterion of stability of characteristic exponents for the two-dimensional linear system through eigen-values and eigen-vectors of its coefficient matrix.

In [26, 27, 30, 31, 35, 46], N. A. Izobov introduced a notion of the minimal exponent of a linear system as the exact lower bound of the highest exponents of linear systems with small perturbations and proposed an algorithm for its calculation in the two-dimensional case, while in the *n*-dimensional case he obtained the lower bound. N. A. Izobov derived [37] calculation formulas for the determined by him in [37, 39,40, 42] the highest and the lowest exponential exponents of the linear system by means of its Cauchy matrix and time geometrical sequences. These exponents are used [40, 42] in solving Lyapunov's special problem on exponential stability according to a linear approximation. N. A. Izobov proved [159, 160] simultaneous instability of lowest and highest exponential exponents of linear differential systems in the following classes of linear perturbations: (1) with characteristic powers equal to $-\infty$; (2) summable on the positive semi-axis with arbitrary power weight. N. A. Izobov introduced [10; see also 57] a notion of highest sigma-exponent of the general linear system as an exact upper bound of highest exponents of linear systems with perturbations exponentially decreasing with velocity $e^{-\sigma t}$, $\sigma > 0$, and, using the Cauchy matrix, he suggested an algorithm of its calculation; later, in [41], jointly with E. Barabanov, he completely described the properties of the abovementioned exponent. The exponential and the sigma-exponents are now called Izobov's exponents. For the set of two-dimensional linear differential systems, N. A. Izobov [79, 80, 83, 90, 119] presented a complete description of mutual disposition of Lyapunov's characteristic exponents, as well as exponential, Vinograd's central and general Bohl exponents.

Starting from his first work [3], N. A. Izobov devoted much attention to the investigation of linear systems with exponentially decreasing perturbations. In particular, in collaboration with O. P. Stepanovich [69, 71, 73, 75], he singled out a class of perturbations and established the existence of linear systems whose characteristic exponents coincide or, respectively, do not coincide with characteristic exponents of linear systems with generalized Grobman perturbations. Moreover, in [76-78, 81], N. A. Izobov proved the stability of highest upward and lowest downward characteristic exponents of linear systems with respect to the same perturbations and established that there exist Grobman spectral sets of positive Lebesgue measure. Jointly with S. G. Krasovskii [126, 130] he gave the description of a method of constructing two-dimensional linear systems with parameter at the derivative and with unbounded with respect to that parameter Lebesgue measure of the spectral sigma-set of characteristic exponents. In [81, 84 and 85], N. A. Izobov obtained attainable deviation estimates of the characteristic exponents of the same type of the initial and the perturbed system with exponentially decreasing perturbations, and in [146, 149, 150], using characteristic exponents of the initial system, he obtained lower bounds of characteristic exponents for linear systems with Perron perturbations. In collaboration with S. N. Batan, he established [147, 148] analogous estimates in the case of the so-called generalized Perron perturbations.

N. A. Izobov gave also a complete description [168, 171] of the relative position on the positive semi-axis of: the coincidence boundary of highest sigma- and characteristic exponents of the linear differential system; its Grobman irregularity coefficient; and the values of the norm of the coefficient matrix. One should also mention the works [5, 6] and those carried out jointly with A. V. Filiptsov [92, 94, 97, 103, 110] dealing with the investigation of invariance of lowest Perron's exponents of solutions of linear systems with respect to exponentially decreasing perturbations, as well as the works [140, 142], where the maximal lower Perron's exponent of the linear system is calculated by means of its fundamental system of solutions.

In a series of works [169, 170, 173, 177, 180, 191] carried out in collaboration with S. A. Mazanik and devoted to systems reducible in Lyapunov's sense: (1) integral criteria of reducibility of a perturbed linear differential system to the initial one are proved and it is established that they are nonimprovable; (2) the notions of the reducibility coefficient and the reducibility exponent of the linear system are introduced, their interconnection is investigated and their attainable boundaries are found that are expressed through the difference of highest and lowest general, central, or exponential indices as well as through the value of norm of the coefficient matrix of that system; (3) the properties of the introduced sets of reducibility and irreducibility of linear systems are thoroughly investigated.

Here it is also worth mentioning the joint with E. K. Makarov solution [60, 68] of Yu. Bogdanov's problem on existence of a regular linear system becoming irregular when its coefficient matrix is multiplied by a positive scalar parameter. Linear periodic systems are treated in N. A. Izobov's works [24, 25, 28 and 29].

The monograph [179] is devoted to a brief and very incomplete exposition of the above-mentioned results of N. A. Izobov as well as of those given in the section below. In that monograph, just as in many of his works, N. A. Izobov systematically applies V. M. Millionshchikov's method of rotations.

Stability According to a Linear Approximation. To investigate exponential stability according to a linear approximation of a differential system with perturbations of order m > 1, N. A. Izobov introduced [9; see also 15] a priori *m*-exponents $\Omega_m(A)$ and constructive *m*-exponents $\Omega''_m(A)$ (the latter computable by means of the Cauchy matrix) of the linear system $\dot{x} = A(t)x, x \in \mathbb{R}^n, t \ge 0$, whose negative values, as functions of the parameter *m*, he completely described [49, 50, 63, 91] by means of uniformly convergent series. We also mention here N. A. Izobov's results [56, 59] concerning the existence of differential systems with exponentially stable linear approximations and perturbations of higher order of smallness, whose set of characteristic and lower exponents are of positive Lebesgue measure. Another properties of these sets have been established by N. A. Izobov in collaboration with I. A. Volkov [64, 65, 67].

As is known (see, e.g., 145, 157, 179, p. 262), there exist the special and the general Lyapunov's problems on the exponential stability according to a linear approximation of the differential system with perturbations, respectively, of unfixed higher order of smallness and of fixed order m > 1.

The solution of the special problem was obtained by N. A. Izobov [40, 42 and 138]: the zero solution of the differential system is exponentially stable with respect to any perturbation of higher order of smallness if and only if the constructive exponent $\Omega''_m(A)$ of the linear approximation system is negative for every m > 1. In the case of the stronger property of exponential stability, this criterion consists [39, 40, 42, 138] in the negativeness of the exponential exponent of the linear approximation system which provides general attainable exponential asymptotics of solutions.

When solving the general Lyapunov's problem, N. A. Izobov, jointly with R. E. Vinograd [13–15], established that R.E. Vinograd's condition $\Omega'_m(A) < 0$ for the estimating exponent $\Omega'_m(A)$ of the linear approximation system is sufficient, while N. A. Izobov's condition $\Omega''_m(A) < 0$ is necessary (see also [9]) for the exponential stability of the differential system with the linear approximation $\dot{x} = A(t)x, x \in \mathbb{R}^n, t \ge 0$, and any perturbation of order m > 1. This fact in the noncritical case when the above-mentioned exponents coincide provides a solution of the general problem. However, in the critical case, as established by N. A. Izobov [52; see also 93] later, these conditions are not, respectively, necessary and sufficient for the exponential stability. Moreover, N. A. Izobov [52] obtained a complete solution of the above-mentioned problem in the case of the linear diagonal approximation. A presentation of the above-obtained results can be found in the review papers [145, 157].

Linear Coppel-Conti's Systems. N. A. Izobov, in collaboration with R. A. Prokhorova, carried out a complete enough investigation [66, 62, 63, 66, 72, 74, 82, 85, 95, 192, 197, 117, 118, 139] of the structure of the

Coppel–Conti sets L^pS and N^pS , $p \ge 1$, of, respectively, asymptotically stable and unstable linear systems with unbounded, in general, coefficients. These systems determine the boundedness of all or of only one solution of inhomogeneous linear systems with corresponding non-homogeneities.

In particular, they solved the first Conti problem on narrowing of the sets L^pS and N^pS , as p > 0 increases, and establised that there exists no continuous from the left dependence of these sets on the parameter p. In [72, 74], criteria are obtained for the coincidence of the sets L^pS and N^pS with their interior, as well as the second Conti problem is solved on the coincidence of the set $\lim_{p \to +\infty} L^pS$ with its interior, as a special case of a more general problem. N. A. Izobov [86, 97], jointly with R. Conti and R. A. Prokhorova, studied thoroughly the preblem on the simultaneous belonging of the initial and perturbed linear systems with summable on $[0, +\infty]$ perturbations to the sets L^pS , as well as to their left and right limiting, at the point p = q, sets.

During the last decade, N. A. Izobov, in collaboration with R. A. Prokhorova, completely described [158, 161, 163] the set of all such asymptotically stable linear differential Coppel-Conti systems and established that the zero solution of every nonlinear system with linear approximation from that set and any perturbation of higher order of smallness is asymptotically stable. They also described [164–166] the set of all unstable linear differential Coppel–Conti systems for which every nontrivial solution of an analogous nonlinear perturbed system, starting from a sufficiently small neighborhood of the origin of coordinates, in a finite time gets to the boundary of that neighborhood. The same authors proved [174, 178, 201] that the highest characteristic exponent and the lowest characteristic exponent of, respectively, asymptotically stable and unstable linear Coppel–Conti systems are, respectively, negative and positive, and obtained their upper and lower bounds. They also proved [163, 182, 201] that the Lyapunov's characteristic exponents are negative for all starting in a sufficiently small neighborhood of the origin solutions of a nonlinear differential system with perturbations of higher order of smallness and with linear asymptotically stable Coppel–Conti approximation. Using a constant defined by means of the linear Coppel–Conti approximation, the upper bound for exponents of these solutions is obtained [163, 182, 201]. Thus a complete solution is presented for Lyapunov's problem on the exponential stability according to the aboveconsidered linear Coppel–Conti approximation.

N. A. Izobov established [186, 192] conditional exponential stability of the zero solution of a multi-dimensional nonlinear differential system with a general integro-dichotomous linear Coppel–Conti approximation and a nonlinear perturbation of higher order of smallness which is piecewise continuous in the time variable and continuous in the phase variables in some neighborhood of the origin of coordinates. The existence of a k-dimensional family of exponentially decreasing (as the time increases) solutions of the above-mentioned nonlinear system is proved, and an upper estimate of characteristic exponents of those solutions is obtained.

The monograph [190] by N. A. Izobov and R. Prokhorova is devoted to the exposition of their results of investigation of properties and structure of a dependent on a parameter set of linear differential Coppel–Conti systems and its main subsets.

The Emden–Fowler Equations. Investigations by N. A. Izobov of the classical equation $u^{(n)} = p(t)|u|^{\lambda} \operatorname{sign} u, n \geq 2, \lambda > 0, t \geq 0$, with a function p(t) of constant sign are initiated by and connected with solving [44, 45, 48] of two I. T. Kiguradze's problems on necessity of well-known existence criteria for the Emden-Fowler equation to have:1) in case $\lambda > 1$, an *n*-parametric family of infinitely right-extendable monotone solutions; 2) in case p(t) satisfies $(-1)^n p(t) \geq 0$ for $t \geq 0$ and $\lambda \in (0, 1)$, vanishing at infinity regular Kneser solutions.

In [44,45], N. A. Izobov obtained a general integral criterion (involving a fractional parametric power of the function $p(t) \geq 0$) for the above equation with $\lambda > 1$ not to have unbounded regular solutions and established that this criterion is non-improvable. Moreover, in [44], for the Emden–Fowler equation of second order he obtained criteria for existence and nonexistence of unbounded regular solutions with an additional differential property. Jointly with V. A. Rabtsevich, N. A. Izobov [54, 58] established that the Kiguradze–Kvinikadze's criterion on existence of regular solutions of the Emden–Fowler equation with $\lambda > 1$ is non-improvable.

In [48], N. A. Izobov obtained a parametric integral criterion of nonexistence of Kneser solutions of the Emden–Fowler equation with $\lambda \in (0, 1)$, and proved its exactness for the case n = 2. Jointly with V. A. Rabtsevich [70] he made somewhat more precise this criterion for $n \geq 3$ and established that it is non-unimprovable.

Linear Pfaff's Systems. In [113, 114, 120, 122, 123, 125, 129, 131, 136], N. A. Izobov, in particular, established that there exist linear completely integrable Pfaff's systems with two-dimensional time, the countable number of different characteristic sets of solutions and with the lower characteristic set (introduced in [114] as an analogue of the set of lower Perron's exponents in the case of one-dimensional time) of positive plane Lebesgue measure. Moreover, N. A. Izobov, in collaboration with A. S. Platonov, [121, 124, 128, 133, 135, 137, 143], established other properties of lower characteristic sets, having proved, in particular, that almost all solutions of the linear Pfaff's system with two-dimensional time starting at an arbitrary k-dimensional subspace of the n-dimensional space, have lower characteristic sets coinciding with the least upper bound of the whole set of lower characteristic vectors of these solutions. Besides, N. A. Izobov jointly with S. G. Krasovskiĭ and A. S. Platonov, proved [193, 197, 198] that there exist n-dimensional completely integrable linear Pfaff's systems with k-dimensional

time and the lower characteristic set of positive Lebesgue measure in the k-dimensional space.

In collaboration with E. N. Krupchik, N. A. Izobov completely described [141, 144, 151, 153] the structure of limiting lower power characteristic sets of nontrivial solutions of linear fully integrable Pfaff's systems with two-dimensional time. They also gave [154] a complete description of the limiting left and right lower and upper power sets of nontrivial solutions of such systems. They constructed [162, 167] a completely integrable linear Pfaff's system with arbitrarily prescribed piecewise continuous characteristic power functions (having, in particular, a countable number of points of discontinuity) of its nontrivial solutions.

Of special interest is the following special result obtained by N. A. Izobov [181]: any two-dimensional linear Pffaff's system with two-dimensional time has at most countable number of solutions with different characteristic sets. As it was pointed out, earlier N. A. Izobov established [122] that linear Pfaff's systems with the countable number of such solutions do exist.

Along with intensive enough theoretical investigations in the asymptotic theory of differential systems, N. A. Izobov carried out a series of investigations of applied character, for example, in the mechanics of motion of objects along surfaces close to spherical ones (see [175, 178, 183, 185, 188, 189, 194-196, 199, 200]).

N. A. Izobov has published more than 200 scientific works. Under N. A. Izobov's supervision over 21 Candidates and Doctors of Sciences defended their theses. He has been Chairman of the Expert Council in Mathematics of the Higher Certifying Commission of Republic of Byelorussia (and is its member at present), a member of Bureau of Physics, Mathematics and Informatics Department of National Academy of Sciences of Byelorussia, a member of Editorial Board of "Central European Journal of Mathematics". At present he is member of editorial boards of the journals "Differentsial'nye Uravneniya", "Memoirs on Differential Equations and Mathematical Physics", "Doklady NAN Belarusi", "Vestsi NAN Belarusi. Ser. Fiz.-Mat. Navuk", Deputy Editor-in-Chief of the journal "Trudy Instituta Matematiki NAN Belarusi".

N. A. Izobov was decorated with Frantsisk Skorina Order and awarded the State Prize of Republic of Byelorussia.

Editorial Board wishes Nikolaĭ Alekseyevich Izobov good health and new successes.

R. P. Agarwal, I. Kiguradze, T. Kiguradze, S. G. Krasovskii, T. Kusano, G. Kvinikadze, A. Lomtatidze, V. P. Maksimov, F. Neuman, N. Partsvania, M. O. Perestyuk, N. Kh. Rozov, A. M. Samoilenko

References

- 1. On the number of lower exponents for the solutions of a linear differential system. (Russian) Dokl. Akad. Nauk BSSR 8 (1964), 761–762.
- On a set of lower indices of a linear differential system. (Russian) Differencial'nye Uravneniya 1 (1965), 469–477.
- Stability with respect to the first approximation. (Russian) Differencial'nye Uravneniya 2 (1966), 898–907.
- 4. Weakly irregular system. (Russian) Differencial'nye Uravneniya 3 (1967), 787-795.
- Asymptotic characteristics of linear and weakly nonlinear systems. (Russian) Tez. dokl. II Resp. Konf. matematikov Belorussii (Abstracts of II Conference of Mathematicians of Republic Byelorussia), Minsk, 1967, part 1, p. 125.
- Asimptoticheskie kharakteristiki lineinykh i slabo nelineinykh sistem (Asymptotic Characteristics of Linear and Weakly Nonlinear Systems). (Russian) Summary of Ph.D. Thesis, Minsk, 1967.
- The set of lower exponents of positive measure. (Russian) Differencial'nye Uravneniya 4 (1968), 1147–1149.
- Linear systems with coefficients of weak variation. (Russian) Tr. II Resp. konf. matematikov Belorussii (Abstracts of II Conference of Mathematicians of Republic Belorussia), Belorussia State University, Minsk, 1969, 182–185.
- The highest exponent of a system with perturbations of order higher than one. (Russian) Vestnik Beloruss. Gos. Univ. Ser. I (1969), No. 3, 6–9.
- The highest exponent of a linear system with exponential perturbations. (Russian) Differencial'nye Uravneniya 5 (1969), 1186–1192.
- Necessary and sufficient conditions for the stability of the characteristic exponents of a diagonal system (with B. F. Bylov). (Russian) *Differencial'nye Uravneniya* 5 (1969), 1785–1793.
- Necessary and sufficient conditions for the stability of the characteristic exponents of a linear system (with B. F. Bylov). (Russian) Differencial'nye Uravneniya 5 (1969), 1794–1803.
- Solution of the Lyapunov stability problem by the first approximation (with R. E. Vinograd). (Russian) Tez. dokl. V Mezhdunar. konf. po nelin. kolebaniyam (Abstracts of V Int. Conf. on Nonlinear Oscillations), Kiev, 1969, 51–52.
- Solution of the Lyapunov stability problem by the first approximation (with R. E. Vinograd). (Russian) Tr. V Mezhdunar. konf. po nelin. kolebaniyam (Proceedings of V Int. Conf. on Nonlinear Oscillations), Kiev, 2 (1970), 121–126.
- Solution of the Ljapunov stability problem by the first approximation (with R. E. Vinograd). (Russian) Differencial'nye Uravneniya 6 (1970), 230–242.
- 16. An integral version and the sharpness of the estimate for the higher exponent in the freezing method. (Russian) Tez dokl. Ill Resp. konf. matematikov Belorussii (Abstracts of III Conf. of Mathematicians of Republic Byelorussia), Minsk, 1971, p. 23.
- A refinement of the estimate in the freezing method for a two-dimensional system with coincident characteristic numbers. (Russian) Differencial'nye Uravneniya 7 (1971), 990–996.
- Cases of sharpening and the attainability of an estimate of the highest exponent in the method of freezing. (Russian) *Differencial'nye Uravneniya* 7 (1971), 1179–1191, 1339–1340.
- Cases of sharpening and attainability of the estimate of the higher exponent in the freezing method. (Russian) Tez. dokl. Vsesoyuz. konf. po kachestv. teorii differents. uravnenii (Abstracts of All-Union Conf. on Qual. Theory of Diff. Eqs.), Ryazan, 1971, p. 128.
- 20. The canonical form of a linear two-dimensional system with variable coefficients. (Russian) Differencial'nye Uravneniya 7 (1971), 2136–2142.

- A coefficient criterion for the stability of the Ljapunov exponents of a twodimensional linear system. (Russian) Ukrain. Mat. Z. 24 (1972), 306–315.
- 22. A generalized Euler method for the integration of a linear system with variable coefficients. (Russian) Differencial'nye Uravneniya 9 (1973), 1001–1018.
- Linear systems of ordinary differential equations. (Russian) Mathematical analysis, Vol. 12 (Russian), pp. 71–146, 468. (loose errata) Akad. Nauk SSSR Vsesojuz. Inst. Naucn. i Tehn. Informacii, Moscow, 1974.
- Half periods of the solutions of two-dimensional linear systems. (Russian) Differencial'nye Uravneniya 11 (1975), No. 5, 782–797.
- 25. The multipliers of a two-dimensional second-order periodic system. (Russian) Tez. dokl. Vsesoyuz. konf. po kachestv. teorii differents. uravnenii (Abstracts of All-Union Conf. on Qual. Theory of Diff. Eqs.), Ryazan, 1976.
- The minimal exponent of a two-dimensional diagonal system. (Russian) Differencial'nye Uravneniya 12 (1976), No. 11, 1954–1966.
- The minimal exponent of a two-dimensional linear differential system. (Russian) Differencial'nye Uravneniya 13 (1977), No. 5, 848–858.
- The extension of the Ljapunov integral criterion to second order two-dimensional periodic systems. (Russian) Mat. Zametki 21 (1977), No. 6, 817–827.
- The absence of real multipliers for an n-dimensional periodic system of order 4m+2. (Russian) Differencial'nye Uravneniya 13 (1977), No. 9, 1581–1587, 1731–1732.
- Lower bound for the minimal exponent of a linear system. (Russian) Differentsial'nye Uravneniya 14 (1978), No. 9, 1576–1588.
- Lower bound for the minimal exponent of a linear system. (Russian) Differentsial'nye Uravneniya 14 (1978), No. 9, 1576–1588.
- 32. K teorii kharakteristicheskikh pokazatelei Lyapunova lineinykh i kvazilineinykh differ-entsial'nykh sistem (A remark to the theory of lyapunov characteristic exponents of linear and quasilinear differential systems). (Russian) Summary of D.Sc. Thesis (phys.-math.), Leningrad State University, Leningrad, 1978.
- On the theory of characteristic Lyapunov exponents of linear and quasilinear differential systems. (Russian) Mat. Zametki 28 (1980), No. 3, 459–476.
- 34. Attainable bounds of characteristic exponents of a two-dimensional linear system. (Russian) Tez. dokl. V Resp. konf. matematikov Belorussii (Abstracts of V Conf. of Mathematicians of Republic Belorussia), Grodno, 1980, part 2, p. 51.
- The minimal exponent of a linear differential system (Russian) Tez. dokl. IX Mezhdunar. konf. po nelin. kolebaniyam (Abstracts of IX Int. Conf. on Nonlin. Oscillations), Kiev, 1981, 137–138.
- 36. The spectrum of characteristic exponents of a two-dimensional stationary system with perturbations-rotations (with T. E. Zvereva). (Russian) Differentsial'nye Uravneniya 17 (1981), No. 11, 1964–1977.
- Exponential indices of a linear system and their calculation. (Russian) Dokl. Akad. Nauk BSSR 26 (1982), No. 1, 5–8.
- Sharp bounds of characteristic exponents of two-dimensional linear systems with bounded perturbations. (Russian) *Differentsial'nye Uravneniya* 18 (1982), No. 5, 767–772.
- The upper bound of the Lyapunov exponents of differential systems with higherorder perturbations. (Russian) Dokl. Akad. Nauk BSSR 26 (1982), No. 5, 389–392.
- Exponential indices and stability in the first approximation. (Russian) Vestsi Akad. Navuk BSSR Ser. Fiz.-Mat. Navuk, 1982, No. 6, 9–16.
- The form of the highest σ-exponent of a linear system (with E. A. Barabanov). (Russian) Differentsial'nye Uravneniya 19 (1983), No. 2, 359–362.
- Exponential exponents and stability in the first approximation. (Russian) Uspekhi Mat. Nauk. 38 (1983), No. 5(233), p. 129.
- Refinement of bounds for highest exponents in the freezing method. (Russian) Differentsial'nye Uravneniya 19 (1983), No. 8, 1454–1456.

- The Emden-Fowler equations with unbounded infinitely continuable solutions. (Russian) Mat. Zametki 35 (1984), No. 2, 189–199.
- Continuable and noncontinuable solutions of a nonlinear differential equation of arbitrary order. (Russian) Mat. Zametki 35 (1984), No. 6, 829–839.
- The minimal exponent of a linear differential system. (Russian) Ninth International Conference on nonlinear Oscillations, Vol. 2 (Kiev, 1981), 147–149, 473, "Naukova Dumka", Kiev, 1984.
- Continuable and noncontinuable solutions of the Emden-Fowler equation. (Russian) Uspekhi Mat. Nauk. 39 (1984), No. 4(238), p. 137.
- 48. Kneser solutions. (Russian) Differentsial'nye Uravneniya 21 (1985), No. 4, 581–588.
- Functions defined by higher-order central exponents. (Russian) Uspekhi Mat. Nauk 40 (1985), No. 4(244), 167–168.
- Properties of higher-order central exponents. (Russian) Differentsial'nye Uravneniya 21 (1985), No. 11, 1867–1884.
- Continuable and noncontinuable solutions of the Emden-Fowler equation. (Russian) Reports of the extended sessions of a seminar of the I. N. Vekua Institute of Applied Mathematics, Vol. I, No. 3 (Russian) (Tbilisi, 1985), 43–46, 166, Tbilis. Gos. Univ., Tbilisi, 1985.
- Stability with respect to linear approximation. Special cases. (Russian) Differentsial'nye Uravneniya 22 (1986), No. 10, 1671–1688.
- Necessary and sufficient properties of higher-order central exponents. (Russian) Tez. dokl. VI Vsesoyuz. konf. po kachestv. teorii differents. uravnenii (Abstracts of VI AH-Union Conf. on Qual. Theory of Diff. Eqs.), Irkutsk, 1986, 80–81.
- 54. The unimprovability of the existence condition for rapidly growing proper solutions of the Emden–Fowler equation (with V. A. Rabtsebich). (Russian) Annotatsii dokl. vsesoyuz. simp. "Sovr. problemy mat. fiziki" (Annotations of Reports of All-Union Symp. "Modern Problems of Math. Physics"), Tbilisi, 1987, 20–21.
- On a problem of R. Conti (with R. A. Prokhorova). (Russian) Differentsial'nye Uravneniya 23 (1987), No. 5, 775–791.
- The measure of the set of characteristic and lower characteristic exponents of differential systems with higher-order perturbations. (Russian) Uspekhi Mat. Nauk. 42 (1987), No. 4(256), 117.
- Properties of the lower sigma-exponent of a linear differential system. (Russian) Uspekhi Mat. Nauk. 42 (1987), No. 4(256), 179.
- The unimprovability of the I. T. Kiguradze-G. G. Kvinikadze condition for the existence of unbounded regular solutions of the Emden-Fowler equation (with V. A. Rabtsevich). (Russian) *Differentsial'nye Uravneniya* 23 (1987), No. 11, 1872–1881, 2019–2020.
- The number of characteristic and lower exponents of an exponentially stable system with higher-order perturbations. (Russian) Differential'nye Uravneniya 24 (1988), No. 5, 784–795, 916–917; English transl.: Differential Equations 24 (1988), No. 5, 510–519.
- 60. Lyapunov irregular linear systems with a parameter multiplying the derivative (with E. K. Makarov). (Russian) Differentsial'nye Uravneniya 24 (1988), No. 11, 1870–1880; English transl.: Differential Equations 24 (1988), No. 11, 1243–1250 (1989).
- The measure of the solution set of a linear system with the largest lower exponent. (Russian) Differentsial'nye Uravneniya 24 (1988), No. 12, 2168–2170.
- Conti sets of linear differential systems (with R. A. Prokhorova). (Russian) Uspekhi Mat. Nauk. 43 (1988), issue 4, 166.
- Linear Conti Systems and Their Generalizations (with R. A. Prokhorova). (Russian) VII Vsesoyuz. konf. "Kachestvennaya teoriya differents. uravnenii", Riga, 3–7 apr. 1989 (Proc. of VII All-Union Conf. "Qual. Theory of Diff. Eqs.", Riga, April 3–7, 1989), Riga, 1989, 107.

- 64. Connectivity components of a set of characteristic exponents of a differential system with higher-order perturbations (with I. A. Volkov). (Russian) Dokl. Akad. Nauk BSSR 33 (1989), No. 3, 197–200.
- 65. A set of lower Perron exponents for a differential system with higher-order perturbations (with I. A. Volkov). (Russian) Dokl. Akad. Nauk BSSR 33 (1989), No. 6, 485–487.
- Unstable linear systems of R. Conti (with R. A. Prokhorova). (Russian) Vestnik Beloruss. Gos. Univ. Ser. I Fiz. Mat. Mekh. 1989, No. 2, 39–44.
- 67. The sets of characteristic and lower exponents of differential systems with higherorder perturbations (with I. A. Volkov). (Russian) Vsesoyuz. konf. "Nelineinye problemy differentsial'nykh uravnenii i matematicheskoi fiziki", Ternopol', 12–15 sent. 1989: Tez. dokl. (Abstr. of All-Union Conf. "Nonlin. Problems of Diff. Eqs. and Math. Physics", Ternopol, September 12–15, 1989), Ternopol, 1989, part 1, 167–168.
- Lyapunov proper linear systems with parameter multiplying the derivative (with E. K. Makarov). (Russian) Uspekhi Mat. Nauk. 44 (1989), No. 4(268), 208–209.
- On the invariance of characteristic exponents of linear systems under exponentially decreasing perturbations (with O. P. Stepanovich). (Russian) Arch. Math. (Brno) 26 (1990), No. 2-3, 107–114.
- Vanishing Kneser solutions of the Emden–Fowler equation (with V. A. Rabtsevich). (Russian) Differentsial'nye Uravneniya 26 (1990), No. 4, 578–585; English transl.: Differential Equations 26 (1990), No. 4, 419–424.
- Exponentially decreasing perturbations that preserve the characteristic exponents of a linear diagonal system (with O. P. Stepanovich). (Russian) Differentsial'nye Uravneniya 26 (1990), No. 6, 934–943; English transl.: Differential Equations 26 (1990), No. 6, 667–675.
- 72. On the Conti problem for intersections of sets L^pS of linear systems (with R. A. Prokhorova). (Russian) Differentsial'nye Uravneniya 26 (1990), No. 8, 1323–1334, 1467–1468; English transl.: Differential Equations 26 (1990), No. 8, 966–975 (1991).
- Properties of the coefficient of nonregularity of linear systems (with O. P. Stepanovich). (Russian) Differentsial'nye Uravneniya 26 (1990), No. 11, 1899–1906; English transl.: Differential Equations 26 (1990), No. 11, 1410–1416 (1991).
- Conti limit sets of linear differential systems (with R. A. Prokhorova). (Russian) Tez. dokl. Resp. nauch. chtenii po obykn. differents. uravneniyam (Abstr. of Repub. Scientific Readings on Ordinary Diff. Eqs.), Minsk: Belarus State University, 1990, p. 57.
- On the coincidence of characteristic sets of linear systems (with O. P. Stepanovich). (Russian) Differentsial'nye Uravneniya 26 (1990), No. 12, 2182.
- Characteristic exponents of linear systems with Grobman perturbations. (Russian) Differentsial'nye Uravneniya 27 (1991), No. 3, 428–437; English transl.: Differential Equations 27 (1991), No. 3, 299–306.
- 77. On the existence of Grobman spectral sets of positive measure for linear systems. (Russian) Differentsial'nye Uravneniya 27 (1991), No. 6, 953–957; English transl.: Differential Equations 27 (1991), No. 6, 666–669.
- The grobman spectral sets of characteristic exponents of linear systems. (Russian) Differentsial'nye Uravneniya 27 (1991), No. 8, 1463–1464.
- Some properties of characteristic and other exponents of two-dimensional linear systems. (Russian) Differentsial'nye Uravneniya 27 (1991), No. 11, 2013–2014.
- Mutual arrangement of characteristic, exponential, central, and singular exponents of two-dimensional linear systems. (Russian) Differentsial'nye Uravneniya 28 (1992), No. 6, 1085.
- On characteristic exponents of linear systems with exponentially decaying perturbations. (Russian) VI konf. matematikov Belarusi, Grodno, 29 sent.-2 okt.

1992, Ch. 3 : Obyknovennye differentsial'nye uravneniya. Matematicheskie problemy mekhaniki (IV Conf. of Mathematician of Belarus, Grodno, September 29– October 2, 1992, Part 3 : Ordinary Differential Equations. Mathematical Problems in Mechanics), Grodno, 1992, p. 36.

- 82. Linear systems with L^p-dichotomy (with R. A. Prokhorova). (Russian) VI konf. matematikov Belarusi, Grodno, 29 sent.–2 okt. 1992, Ch. 3 : Obyknovennye differentsial'nye uravneniya. Matematicheskie problemy mekhaniki (IV Conf. of Mathematician of Belarus, Grodno, September 29–October 2, 1992, Part 3 : Ordinary Differential Equations. Mathematical Problems in Mechanics), Grodno, 1992, p. 37.
- On the distribution of characteristic and other exponents of two-dimensional linear systems. (Russian) Differential'nye Uravneniya 28 (1992), No. 10, 1683–1698; English transl.: Differential Equations 28 (1992), No. 10, 1366–1380 (1993).
- Estimates for Lyapunov exponents of linear systems with exponentially decaying perturbations. (Russian) Differentsial'nye Uravneniya 28 (1992), No. 11, 2013.
- Estimates for characteristic Lyapunov exponents of linear systems with exponentially decreasing perturbations. (Russian) Differential'nye Uravneniya 28 (1992), No. 12, 2036–2048; English transl.: Differential Equations 28 (1992), No. 12, 1684–1694 (1993).
- Conti-Coppel Sets of linear systems with integrable perturbations (with R. A. Prokhorova). (Russian) Uspekhi Mat. Nauk. 48 (1993), No. 4, 199–200.
- On the linear systems L^pS with summable perturbations (with R. Conti and R. A. Prokhorova). (Russian) Differentsial'nye Uravneniya 29 (1993), No. 10, 1689–1698; English transl.: Differential Equations 29 (1993), No. 10, 1466–1474 (1994).
- Polynomials realized by higher-order central exponents. (Russian) Differentsial'nye Uravneniya 29 (1993), No. 11, 2034.
- Investigations in Belarus in the theory of characteristic Lyapunov exponents and its applications. (Russian) Differentsial'nye Uravneniya 29 (1993), No. 12, 2034–2055 (1994); English transl.: Differential Equations 29 (1993), No. 12, 1771–1788 (1994).
- Joint distribution of characteristic, exponential, central, and singular exponents of linear systems. (Russian) Uspekhi. Mat. Nauk. 49 (1994), No. 4, 96.
- Polynomial representations of higher-order central exponents. (Russian) Differentsial'nye Uravneniya **30** (1994), No. 9, 1508–1515; English transl.: Differential Equations **30** (1994), No. 9, 1395–1401 (1995).
- 92. Lower Perron exponents of linear systems with diagonal approximation and with exponentially decreasing perturbations (with A. V. Filiptsov). (Russian) Differentsial'nye Uravneniya **31** (1995), No. 2, 197–205; English transl.: Differential Equations **31** (1995), No. 2, 182–188.
- 93. On the asymptotic stability and absolute integrability on the semiaxis of solutions of a differential system with perturbations of higher order. (Russian) Differentsial'nye Uravneniya **31** (1995), No. 3, 417–421; English transl.: Differential Equations **31** (1995), No. 3, 385–388.
- 94. Smallness of perturbations preserving perron exponents of linear diagonal systems (with A. V. Filiptsov). (Russian) *Differentsial'nye Uravneniya* **31** (1995), No. 4, 908–909.
- 95. The structure of the interior of Conti-Coppel sets (with R. A. Prokhorova). (Russian) Mat. konf. "Eruginskie Chteniya-II", Grodno, 11–13 maya, 1995. (Math. Conf. "2nd Erugin Readings", Grodno, May 11–13, 1995), Grodno, 1995, p. 54.
- Proper solutions of the Emden-Fowler equation. Int. Conf. "Nonlinear Differential Equations", Kiev, August 21–27, Kiev, 1995, p. 63.
- On the sharpness of conditions for the coincidence of lower Perron exponents of linear differential systems (with A. V. Filiptsov). (Russian) *Differ. Uravn.* **31** (1995), No. 8, 1300–1309; English transl.: *Differential Equations* **31** (1995), No. 8, 1244–1252 (1996).

- Criteria for the absence of unbounded proper solutions of the second-order Emden– Fowler equation. (Russian) Differ. Uravn. 31 (1995), No. 11, 1934.
- 99. Unbounded proper solutions of the emden-fowler equation of an arbitrary order. (Russian) Vtorye Resp. nauchn. chteniya po obyknovennym differents. uravneniyam, posvyashch. 75-letiyu Yu.S. Bogdanova, 5-7 dek., 1995 (2nd Repub. Sci. Readings on Ordinary Diff. Eqs. dedicated to the 75th Birthday of Yu. S. Bogdanov, December 5-7, 1995), Minsk, 1995, p. 39.
- 100. Instability of the higher exponent of a linear system under perron perturbations (with S. N. Batan). (Russian) Vtorye resp. nauchn. chteniya po obyknovennym differents. uravneniyam, posvyashch. 75-letiyu Yu.S. Bogdanova, 5-7 dek., 1995 (2nd Repub. Sci. Readings on Ordinary Diff. Eqs. dedicated to the 75th Birthday of Yu.S. Bogdanov, December 5-7, 1995), Minsk, 1995, 11.
- 101. On the absence of unbounded regular solutions of the second-order Emden-Fowler equation. (Russian) Differ. Uravn. 32 (1996), No. 3, 311–316; English transl.: Differential Equations 32 (1996), No. 3, 315–320.
- 102. Bounded solutions of linear nonhomogeneous perturbed systems (with R. A. Prokhorova). (Russian) Mat. konf. "Eruginskie Chteniya-III", Brest, 14–16 maya, 1996 (Math. Conf. "3rd Erugin Readings", Brest, May 14–16, 1996), Brest, 1996, 32.
- 103. On the invariance of lower perron exponents of linear systems under exponentially decaying perturbations (with A. V. Filiptsov). (Russian) *Differ. Uravn.* **32** (1996), No. 6, 853.
- The Characteristic Exponents of Linear Differential Systems with Perron Perturbations (with S. N. Batan). (Russian) Differ. Uravn. 32 (1996), No. 6, 858.
- 105. On the instability of characteristic exponents of linear differential systems under Perron perturbations (with S. N. Batan). (Russian) Differ. Uravn. **32** (1996), No. 10, 1341–1347; English transl.: Differential Equations **32** (1996), No. 10, 1337–1343 (1997).
- 106. Linear systems with exponentially decaying perturbations. (Russian) Tez. dokl. VII Bel. mat. konf. 18–22 noyab., 1996 (Abstr. VII Belarus Math. Conf., November 18–22, 1996), Minsk, 1996, part 2, 63–64.
- 107. The bounded solutions of linear inhomogeneous systems (with R. A. Prokhorova). (Russian) Tez. dokl. VII Bel. mat. konf., 18–22 noyab., 1996 (Abstr. VII Belarus Math. Conf., November 18–22, 1996), Minsk, 1996, part 2, 64–65.
- 108. Unimprovable conditions for the absence of unbounded nonoscillating solutions of the Emden–Fowler equation. (Russian) Uspekhi Mat. Nauk 51 (1996), No. 5, 187.
- Investigations in Belarus in the asymptotic theory of differential systems. (Russian) Vesn. Vitsebsk. dzyarzh. un-ta. (1997), No. 1(3), 48–56.
- On the invariance of perron lower exponents of linear systems under exponentially decaying perturbations (with A. V. Filiptsov). (Russian) *Differ. Uravn.* 33 (1997), No. 2, 177–184.
- 111. On a lower exponent of a two-dimensional linear system with Perron perturbations. (Russian) Differ. Uravn. 33 (1997), No. 5, 623–631; English transl.: Differential Equations 33 (1997), No. 5, 626–634 (1998).
- 112. Characteristic and lower exponents of linear systems with exponentially decaying perturbations. (Russian) Tez. dokl. mezhdunar. mat. konf. "Eruginskie Chteniya-IV", Vitebsk, 20–22 maya, 1997. (Abstr. Int. Math. Conf. "4th Erugin Readings", Vitebsk, May 20–22, 1997), Vitebsk, 1997, 38–39.
- Linear Pfaff systems with lower characteristic set of positive plane measure. (Russian) Differ. Uravn. 33 (1997), No. 11, 1570.
- 114. On the existence of linear Pfaffian systems whose set of lower characteristic vectors has a positive plane measure. (Russian) *Differ. Uravn.* **33** (1997), No. 12, 1623–1630; English transl.: *Differential Equations* **33** (1997), No. 12, 1626–1632 (1998).

- 115. Estimates of the lower exponent of the two-dimensional linear system under perron perturbations. Mem. Differential Equations Math. Phys. 11 (1997), 170–173.
- 116. On the exactness of upper estimates of the characteristic exponent of a linear system with exponentially decreasing perturbations (with S. N. Batan). Mem. Differential Equations Math. Phys. 11 (1997), 174–177.
- 117. Coppel-Conti sets of linear systems (with R. A. Prokhorova). Mem. Differential Equations Math. Phys. 12 (1997), 90–98.
- 118. Coppel-Conti sets of linear systems (with R. A. Prokhorova). (Russian) Differential Equations and Mathematical Physics. Int. Symp. dedicated to the 90th birthday anniversary of academician I. Vekua, June 21–25, Tbilisi, 1997, p. 20.
- 119. A description of the mutual arrangement of exponents of two-dimensional linear differential systems. I. (Russian) *Differ. Uravn.* **34** (1998), No. 2, 166–174; English transl.: *Differential Equations* **34** (1998), No. 2, 170–177.
- 120. On the countability of the number of distinct characteristic sets of solutions of a linear Pfaff system. (Russian) Tez. dokl. mezhdunar. mat. konf. "Eruginskie Chteniya-V", Mogilev, 26–28 maya 1998. (Abstr. Int. Math. Conf. "5th Erugin Readings", Mogilev, May 26–28, 1998), Mogilev, 1998, part 1, 48–50.
- 121. Joint description of the characteristic and lower characteristic sets of a solution of a linear Pfaff system (with A. S. Platonov). (Russian) Tez. dokl. mezhdunar. mat. konf. "Eruginskie Chteniya-V", Mogilev, 26–28 maya 1998. (Abstr. Int. Math. Conf. "5th Erugin Readings", Mogilev, May 26–28, 1998), Mogilev, 1998, part 1, 50–52.
- 122. On the existence of a linear Pfaffian system with a countable number of distinct characteristic sets of solutions. (Russian) *Differ. Uravn.* **34** (1998), No. 6, 735–743; English transl.: *Differential Equations* **34** (1998), No. 6, 732–740.
- 123. On the number of distinct characteristic solution sets of a linear Pfaff system. (Russian) *Differentsial'nye Uravneniya***34** (1998), No. 6, 849.
- 124. On the construction of arbitrary characteristic and lower characteristic sets of a solution of a Pfaff system (with A. S. Platonov). (Russian) *Differentsial'nye Uravneniya* 34 (1998), No. 6, 851–852.
- 125. Calculation of Characteristic and Lower Characteristic Vectors of Solutions of a Pfaff System Along Sequences. (Russian) Differ. Uravn. 34 (1998), No. 6, 857–858.
- 126. On the existence of a linear singular system with an exponential characteristic set of unbounded measure (with S. G. Krasovskii). (Russian) Differ. Uravn. 34 (1998), No. 8, 1049–1055; English transl.: Differential Equations 34 (1998), No. 8, 1052– 1059 (1999).
- 127. The characteristic and lower characteristic sets of a linear Pfaff system. (Russian) Uspekhi Mat. Nauk 53 (1998), No. 4(322), 145.
- 128. Construction of a linear Pfaff equation with arbitrarily given characteristics and lower characteristic sets (with A. S. Platonov). (Russian) *Differ. Uravn.* **34** (1998), No. 12, 1596–1603; English transl.: *Differential Equations* **34** (1998), No. 12, 1600– 1607 (1999).
- Linear Pfaff systems with the lower characteristic vectors' set of positive Lebesgue measure. Mem. Differential Equations Math. Phys. 13 (1998), 136–139.
- On existence of a measure unbounded exponential spectral quantization on symplectic manifolds (with S. G. Krasovskii). Mem. Differential Equations Math. Phys. 13 (1998), 140–144.
- On the enumerable set of different characteristic sets of solutions of a Pfaffian linear system. Mem. Differential Equations Math. Phys. 15 (1998), 153–156.
- 132. Research at the Institute of Mathematics of the Belarus Academy of Sciences on differential and multiparameter systems (with I. V. Gaĭshun). (Russian) Vestsi Nats. Akad. Navuk Belarusi Ser. Fiz.-Mat. Navuk 1998, No. 4, 5–19, 141.
- 133. On the existence of a linear Pfaffian system with a disconnected lower characteristic set of positive measure (with A. S. Platonov). (Russian) *Differ. Uravn.* **35** (1999), No. 1, 65–71; English transl.: *Differential Equations* **35** (1999), No. 1, 64–70.

- 134. On two problems of Kiguradze for Emden-Fowler equations (with V. A. Rabtsevich). (Russian) Nonlinear analysis and related problems (Russian), 73–91, Tr. Inst. Mat. (Minsk), 2, Natl. Akad. Nauk Belarusi, Inst. Mat., Minsk, 1999.
- 135. Metric properties of the set of solutions of a linear Pfaff system with pairwise distinct lower characteristic sets (with A. S. Platonov). (Russian) Tez. dokl. mezhdunar. mat. konf. "Eruginskie Chteniya-V", Gomel', 20–21 maya 1999. (Abstr. Int. Math. Conf. "5th Erugin Readings", Gomel, May 20–21, 1999), Gomel, 1999, part 1, 31–32.
- 136. On time sequences that realize characteristic and lower characteristic vectors of solutions. (Russian) Differ. Uravn. 35 (1999), No. 6, 738–744; English transl.: Differential Equations 35 (1999), No. 6, 739–744.
- 137. The distributions of lower characteristic sets of solutions of a linear Pfaff system in the phase space (with A. S. Platonov). (Russian) *Differ. Uravn.* **35** (1999), No. 11, 1579.
- Lyapunov problems on stability by linear approximation. Advances in stability theory at the end of the 20th century, 17–39, Stability Control Theory Methods Appl., 13, Taylor & Francis, London, 2000.
- Coppel-Conti sets of linear systems (with R. A. Prokhorova). (Russian) Tr. In-ta matematiki NAN Belarusi 4 (2000), 54–68.
- On the maximal lower perron exponent of a linear system (with A. V. Filiptsov). Differ. Uravn. 36 (2000), No. 6, 952–953.
- 141. On the construction of boundary lower power-law sets of solutions of Pfaff linear systems (with E. N. Krupchik). *Differ. Uravn.* **36** (2000), No. 11, 1734–1735.
- 142. On the computation of the maximal lower Perron exponent of a linear system (with A. V. Filiptsov). (Russian) *Differ. Uravn.* **36** (2000), No. 11, 1566–1567; English transl.: *Differ. Equ.* **36** (2000), No. 11, 1719–1721.
- 143. On the measure of the set of solutions of a linear Pfaffian system with coinciding lower characteristic sets (with A. S. Platonov). (Russian) *Differ. Uravn.* **36** (2000), No. 12, 1599–1606; English transl.: *Differ. Equ.* **36** (2000), No. 12, 1754–1761.
- 144. On necessary properties of boundary degree sets of solutions of linear Pfaffian systems (with E. N. Krupchik). (Russian) *Differ. Uravn.* **37** (2001), No. 5, 616–627, 717; English transl.: *Differ. Equ.* **37** (2001), No. 5, 647–658.
- 145. Exponential stability in the linear approximation. (Russian) Differ. Uravn. 37 (2001), No. 8, 1011–1027; English transl.: Differ. Equ. 37 (2001), No. 8, 1057–1073
- 146. On characteristic exponents of linear systems with Perron perturbations. *Differ. Equ.* 37 (2001), No. 11, 1656–1657.
- 147. The characteristic exponents of a linear differential system with generalized Perron perturbations (with S. N. Batan). *Differ. Equ.* **37** (2001), No. 11, 1660–1661.
- 148. Lower bounds for the characteristic exponents of a linear system with generalized Perron perturbations (with S. N. Batan). (Russian) *Differ. Uravn.* **37** (2001), No. 12, 1593–1598; English transl.: *Differ. Equ.* **37** (2001), No. 12, 1670–1676.
- 149. Lower bounds for the characteristic exponents of a linear differential system with Perron perturbations. (Russian) *Differ. Uravn.* **38** (2002), No. 5, 596–602; English transl.: *Differ. Equ.* **38** (2002), No. 5, 626–632.
- 150. Lower bounds for the Lyapunov exponents of linear differential systems under perron perturbations. *Differ. Equ.* **38** (2002), No. 6, 915.
- 151. Construction of an arbitrary boundary lower degree set of the solution of a linear Pfaffian system (with E. N. Krupchik). (Russian) *Differ. Uravn.* **38** (2002), No. 10, 1310–1321; English transl.: *Differ. Equ.* **38** (2002), No. 10, 1393–1405.
- Lemmas on the characteristic set of a linear combination of solutions of a Pfaff linear system, I. Differ. Equ. 38 (2002), No. 11, 1670–1671.
- 153. Description of boundary lower degree sets of solutions of a Pfaff linear system (with E. N. Krupchik). *Differ. Equ.* 38 (2002), No. 11, 1677.

- 154. A joint description of the boundary degree sets of the solution of a linear Pfaffian system. I (with E. N. Krupchik). (Russian) *Differ. Uravn.* **39** (2003), No. 3, 308–319; English transl.: *Differ. Equ.* **39** (2003), No. 3, 331–343.
- 155. A joint description of the boundary degree sets of the solution of a linear Pfaffian system. II (with E. N. Krupchik). (Russian) *Differ. Uravn.* **39** (2003), No. 4, 453–464; English transl.: *Differ. Equ.* **39** (2003), No. 4, 485–496.
- 156. Lemmas on the characteristic set of a linear combination of solutions of a Pfaff linear system. II. Differ. Equ. 39 (2003), No. 6, 910–911.
- 157. Lyapunov problems on stability by linear approximation. Advances in stability theory at the end of the 20th century, 25–48, Stability Control Theory Methods Appl., 13, Taylor & Francis, London, 2003.
- 158. Copel-Konti sets of linear differential systems (with R. A. Prokhorova). Special issue dedicated to Victor A. Pliss on the occasion of his 70th birthday. J. Dynam. Differential Equations 15 (2003), No. 2-3, 281–303.
- 159. On the noninvariance of exponential exponents of linear differential systems under perturbations. *Differ. Equ.* **40** (2004), No. 6, 917.
- On the simultaneous instability of exponential indices of linear differential systems. (Russian) Differ. Uravn. 40 (2004), No. 8, 1023–1032; English transl.: Differ. Equ. 40 (2004), No. 8, 1086–1095.
- On asymptotic stability and instability of differential system with Coppel-Conti linear approximation (with R. A. Prokhorova). Nonlin. Dynamics and Control. 2004, No. 4, 141–152.
- 162. The existence of the linear Pfaff system with piecewise continuous characteristic degree functions (with E. N. Krupchik). Mem. Differential Equations Math. Phys. 32 (2004), 143–146.
- 163. Description of a class of asymptotically stable differential systems with Coppel-Conti linear approximations (with R. A. Prokhorova). *Differ. Equ.* 40 (2004), No. 11, 1654–1655.
- 164. On unstable differential systems with Coppel–Conti linear approximation (with R. A. Prokhorova). Differ. Equ. 40 (2004), No. 11, 1660–1661.
- 165. Asymptotic stability of a differential system with linear Coppel–Conti approximation (with R. A. Prokhorova). (Russian) Differ. Uravn. 40 (2004), No. 12, 1608– 1614; English transl.: Differ. Equ. 40 (2004), No. 12, 1687–1693.
- 166. On solutions of a differential system with an unstable Coppel–Conti linear approximation (with R. A. Prokhorova). (Russian) *Differ. Uravn.* 41 (2005), No. 1, 61–72; English transl.: *Differ. Equ.* 41 (2005), No. 1, 61–73.
- 167. Construction of a Pfaffian system with arbitrary piecewise-continuous characteristic power functions (with E. N. Krupchik). (Russian) *Differ. Uravn.* **41** (2005), No. 2, 177–185; English transl.: *Differ. Equ.* **41** (2005), No. 2, 184–194.
- 168. On the coincidence boundary of higher Sigma- and characteristic exponents of a linear differential system. *Differ. Equ.* **41** (2005), No. 6, 900–901.
- On the reducibility of linear differential systems under exponentially decreasing perturbations (with S. A. Mazanik). *Differ. Equ.* 41 (2005), No. 6, 904–905.
- On the reducibility coefficient of a linear differential system (with S. A. Mazanik). Differ. Equ. 41 (2005), No. 11, 1653–1654.
- 171. On the smallness of perturbations that preserve the highest exponent of a linear differential system. (Russian) *Differ. Uravn.* **41** (2005), No. 12, 1592–1596; English transl.: *Differ. Equ.* **41** (2005), No. 12, 1664–1668.
- 172. Dichotomies in the stability theory (with R. A. Prokhorova). (Russian) IV Bogdanov chten. po obykn. differents. uravn. Tez. dokl. mezhd. konf. Minsk, 7–10 dek. 2005. Inst. matem. NAN Belarusi, Minsk, 2005, 35–39.
- 173. On asymptotically equivalent linear systems under exponentially decaying perturbations (with S. A. Mazanik). (Russian) *Differ. Uravn.* 42 (2006), No. 2, 168–173; English transl.: *Differ. Equ.* 42 (2006), No. 2, 182–187.

- 174. On the integrals of three-dimensional linear differential systems with skewsymmetric matrices of coefficients (with S. E. Karpovich, L. G. Krasnevskii, and E. A. Barabanov). (Russian) *Differ. Uravn.* 42 (2006), No. 8, 1027–1034; English transl.: *Differ. Equ.* 42 (2006), No. 8, 1086–1094.
- 175. Estimates for characteristic and lower exponents of solutions of Coppel–Conti linear systems (with R. A. Prokhorova). *Differ. Equ.* **42** (2006), No. 11, 1646–1647.
- 176. On the Lyapunov characteristic exponents and the lower Perron exponents of solutions of Coppel–Conti linear differential systems (with R. A. Prokhorova). (Russian) *Differ. Uravn.* 42 (2006), No. 12, 1612–1625; English transl.: *Differ. Equ.* 42 (2006), No. 12, 1682–1695.
- 177. On quasiintegrals of non-stationary three-dimensional linear differential systems with antisymmetric coefficient matrix (with S. E. Karpovich, L. G. Krasnevskii, and E. A. Barabanov). *Mem. Differential Equations Math. Phys.* **39** (2006), 149– 153.
- 178. A coefficient of reducibility of linear differential systems (with S. A. Mazanik). Mem. Differential Equations Math. Phys. 39 (2006), 154-157.
- 179. Introduction into the theory of the lyapunov exponents. *Bel. Gos. Univer., Minsk*, 2006. 320 pp.
- 180. A general test for the reducibility of linear differential systems, and the properties of the reducibility coefficient (with S. A. Mazanik). (Russian) *Differ. Uravn.* 43 (2007), No. 2, 191–202; English transl.: *Differ. Equ.* 43 (2007), No. 2, 196–207.
- 181. On the countability of the number of solutions of a two-dimensional linear Pfaff system with different characteristic sets. (Russian) Ukrain. Mat. Zh. 59 (2007), No. 2, 172–189; English transl.: Ukrainian Math. J. 59 (2007), No. 2, 180–196.
- 182. The exponential stability and instability of differential systems with respect to the linear Coppel–Conti approximation. Estimation of characteristic exponents (with R. A. Prokhorova). *Georgian Math. J.* 14 (2007), No. 2, 279–288.
- Differential systems with a linear L^p-dichotomous Coppel-Conti approximation. Differ. Equ. 43 (2007), No. 6, 880–881.
- 184. Transparent microspheres pattern generation in a liquid by counter-propagating beams of laser radiation (with A. A. Afanasév, A. N. Rubinov, V. M. Volkov, and S. Yu. Mikhnevich). Nonlinear Phenomena in Complex Systems 10 (2007), No. 3, 1–6.
- 185. Quasi-integrals of three-dimensional linear differential systems with skew-symmetric coefficient matrices (with S. E. Karpovich, L. G. Krasnevskii, and A. V. Lipnitskii). *Mem. Differential Equations Math. Phys.* **41** (2007), 157–162.
- 186. Asymptotic properties of nonoscillatory proper solutions of the Emden-Fowler equation (with V. A. Rabtsevich). Int. J. Appl. Math. Stat. 9 (2007), No. J07, 55–76.
- 187. Estimates for quasi-integrals of four-dimensional linear differential systems with skew-symmetric coefficient matrices (with S. E. Karpovich, L. G. Krasnevskii, and A. V. Lipnitskii). *Differ. Equ.* 43 (2007), No. 11, 1619–1621.
- 188. Estimates for quasi-integrals of three-dimensional linear differential systems with skew-symmetric coefficient matrices (with S. E. Karpovich, L. G. Krasnevskii, and A. V. Lipnitskii). *Differ. Equ.* **43** (2007), No. 11, 1618–1619.
- 189. Quasi-integrals of three- and four-dimensional linear differential systems with skewsymmetric coefficient matrices (with S. E. Karpovich, L. G. Krasnevskii, and A. V. Lipnitskii). (Russian) *Differ. Uravn.* 43 (2007), No. 12, 1606–1617; English transl.: *Differ. Equ.* 43 (2007), No. 12, 1648–1659.
- Coppel-Conti linear differential systems (with R. A. Prokhorova). Belorus. nauka, Minsk, 2008. 230 p.
- 191. On a property of the reducibility exponent of linear differential systems (with S. A. Mazanik). (Russian) Differ. Uravn. 44 (2008), No. 3, 323–328; English transl.: Differ. Equ. 44 (2008), No. 3, 334–340.

- 192. Conditional exponential stability of a differential system with the linear dichotomous Coppel–Conti approximation. (Russian) Differ. Uravn. 44 (2008), No. 5, 599–612; English transl.: Differ. Equ. 44 (2008), No. 5, 618–631.
- 193. Existence of linear pfaffian systems whose lower characteristic set has positive measure in R³ (with S. G. Krasovskii and A. S. Platonov). Differ. Equ. 44 (2008), No. 10, 1367–1374.
- 194. Construction of eigenvectors of a skew-symmetric matrix and an estimate of their derivatives (with S. E. Karpovich, L. G. Krasnevskii, and A. V. Lipnitskii). *Differ. Equ.* 44 (2008), No. 11, 1641–1642.
- 195. Estimates for quasi-integrals of even-dimensional linear differential systems with skew-symmetric coefficient matrices (with S. E. Karpovich, L. G. Krasnevskii, and A. V. Lipnitskii). *Differ. Equ.* 44 (2008), No. 11, 1646–1647.
- 196. Quasi-integrals of even-dimensional linear differential systems with skew-symmetric coefficient matrices (with S. E. Karpovich, L. G. Krasnevskii, and A. V. Lipnitskii). *Differ. Equ.* 44 (2008), No. 12, 1659–1672.
- 197. On existence of linear Pfaffian systems whose lower characteristic sets has positive Lebesgue *m*-measure (with S. G. Krasovskii and A. S. Platonov). (Russian) *Differ. Uravn.* 45 (2009), No. 5, 635–646.
- 198. Linear Pfaffian systems whose lower characteristic set has positive Lebesgue mmeasure (with S. G. Krasovskii and A. S. Platonov). (Russian) Differ. Uravn. 45 (2009), No. 6, 903.
- 199. Joint estimations of quasiintegrals of three dimensional scew-symmetryc differential systems (with S. E. Karpovich, L. G. Krasnevskii, and A. V. Lipnitskii). (Russian) *Differ. Uravn.* 45 (2009), No. 6, 908–910.
- 200. Joint estimations of quasiintegrals of three dimensional scew-symmetryc differential systems (with S. E. Karpovich, L. G. Krasnevskii, and A. V. Krasnevskii). (Russian) *Differ. Uravn.* 45 (2009), No. 10, 1383–1391.
- 201. Lower bounds of the lowest exponent of Coppel–Conti stable linear system with exponentially decreasing perturbations (with R. A. Prokhorova). (Russian) *Differ. Uravn.* 45 (2009), No. 11, 1400.